VICTORIA UNIVERSITY OF WELLINGTON
TE HERENGA WAKA

AIML 231/DATA 302 — Week 6

Feature Construction

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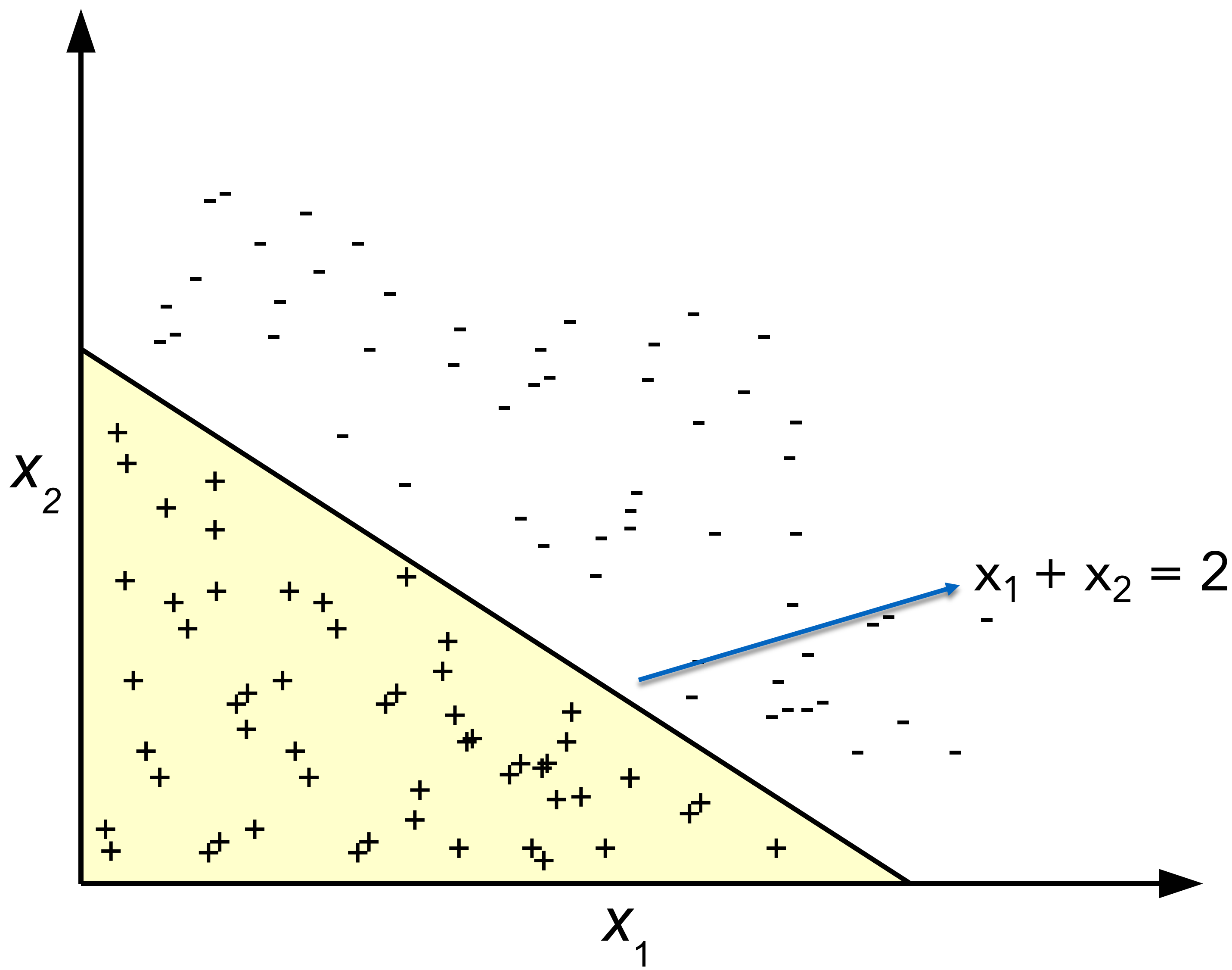
Overview

- What is Feature Construction
- Why Feature Construction
- Feature Construction Process
- Feature Construction Approaches

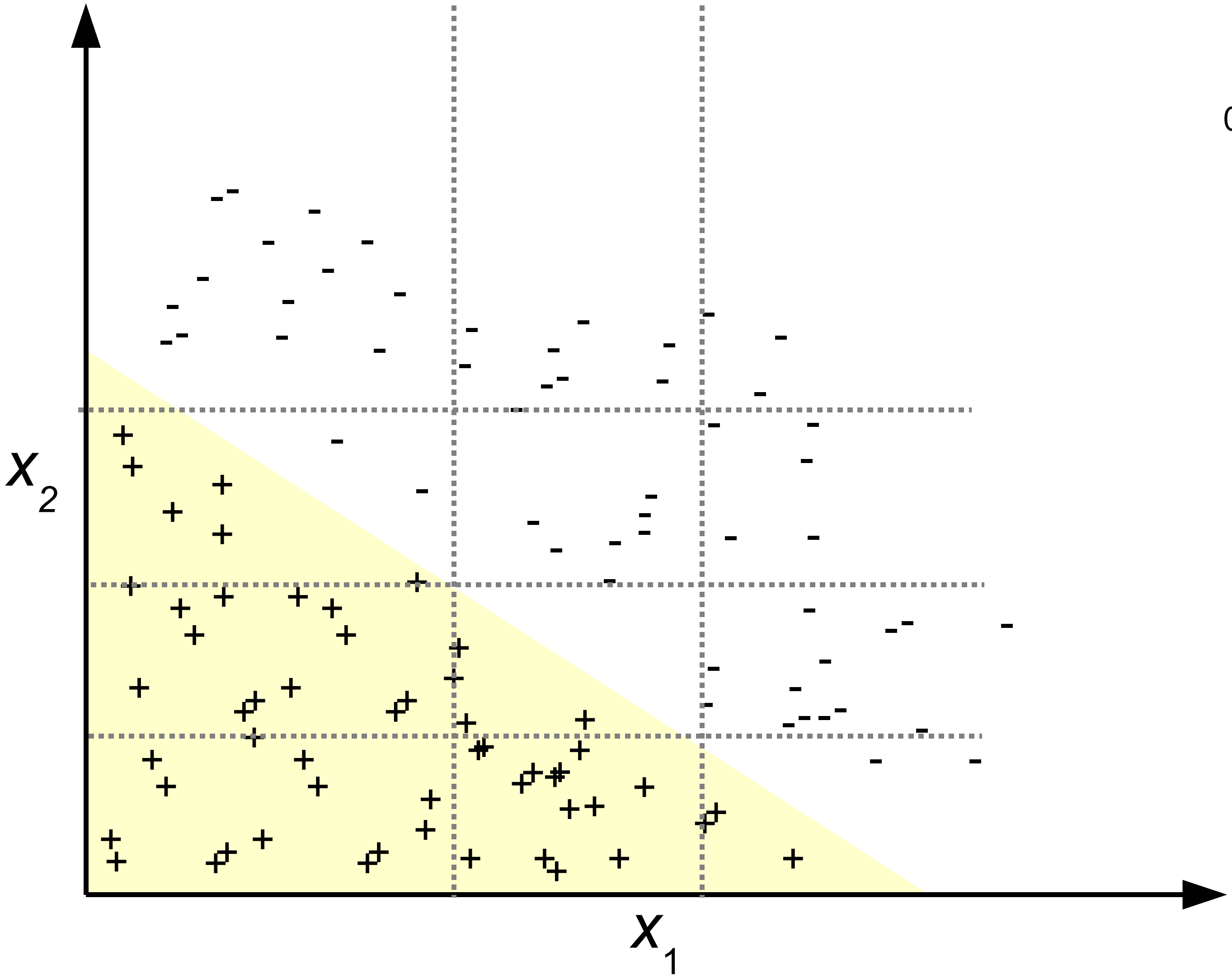
What is a good feature?

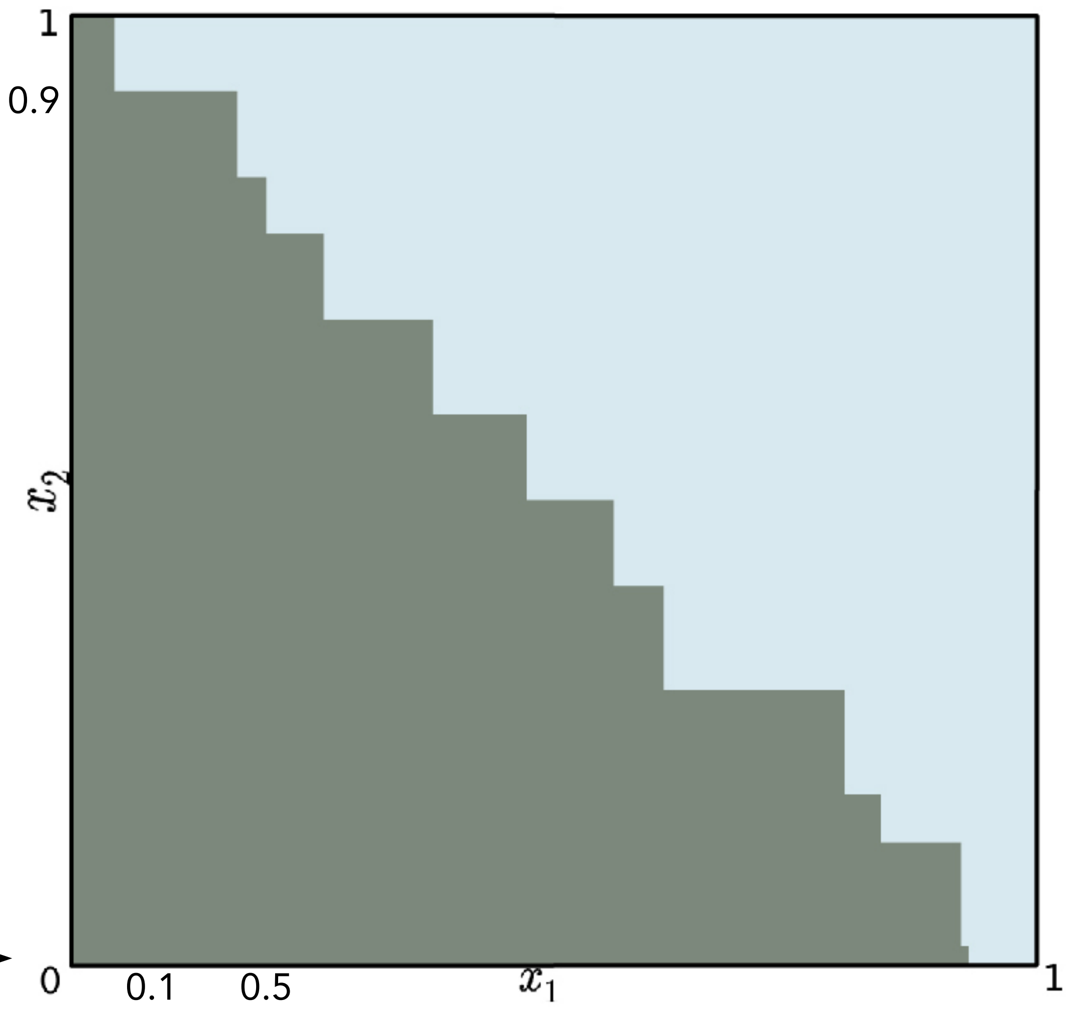
- The measure of goodness is subjective: depends on the problem. The features below are good for a *linear classifier*



What is a good feature?

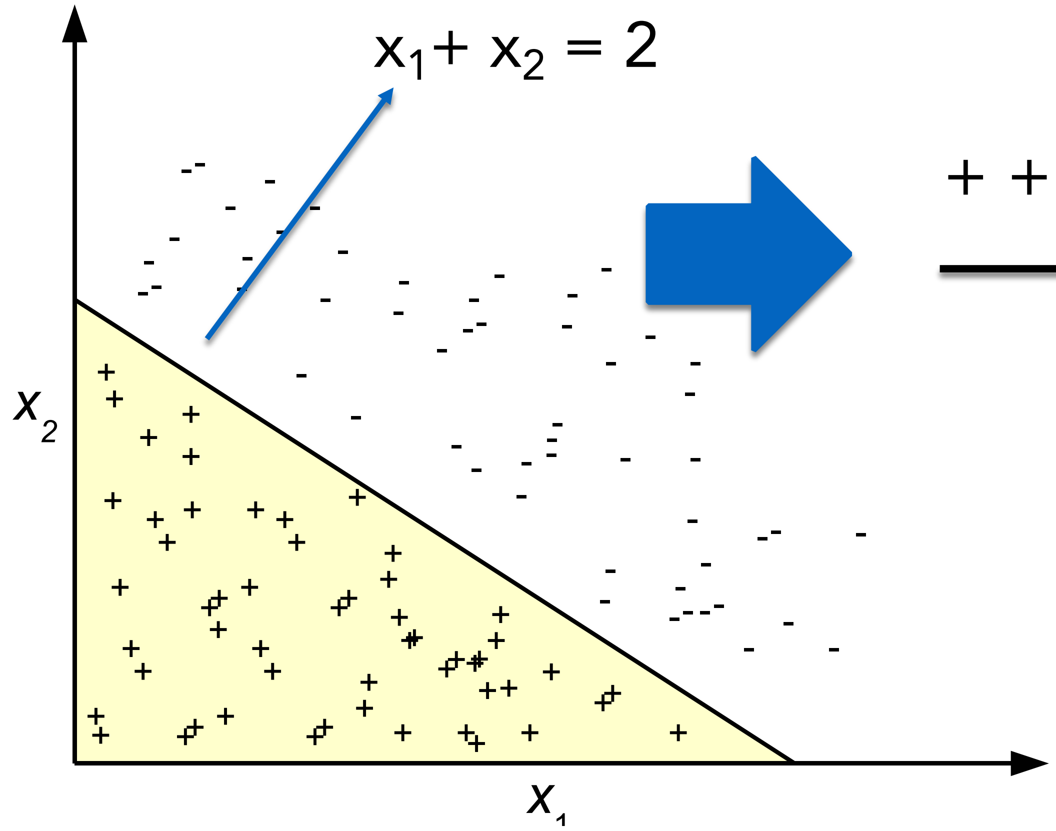
- The same set of features are not good for a DT classifier that is not able to transform its input space

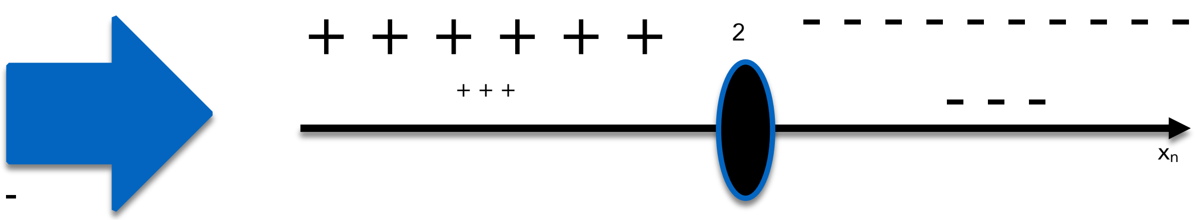




What is a good feature?

New feature: $x_n = x_1 + x_2$: constructed feature





If $x_n > 2$: class –
Else : class +

Why Feature Construction?

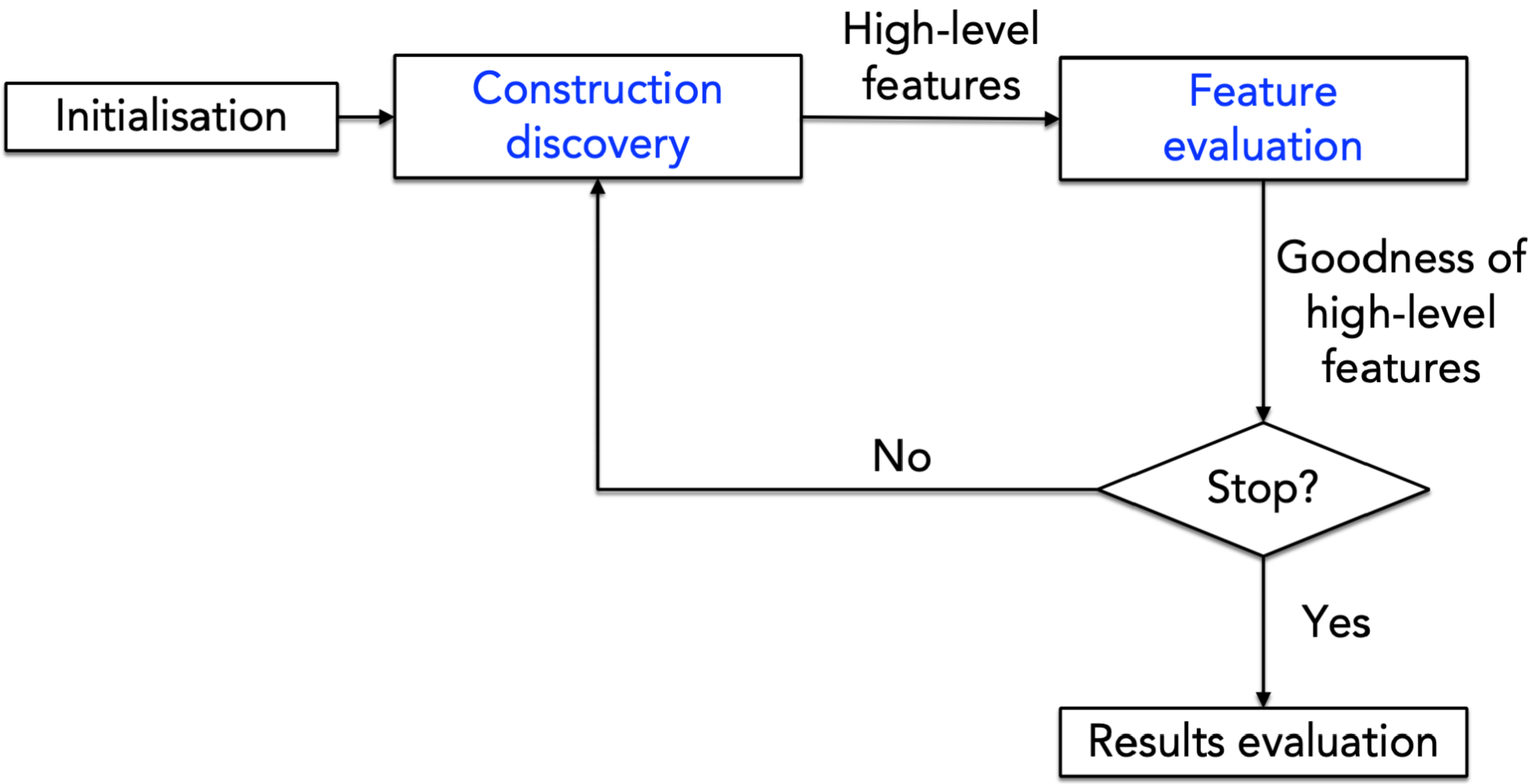
- The quality of input features can drastically affect the learning performance
- Even if the original features are high-quality, transformations may be needed to use them with certain types of classifiers
- A large number of classification algorithms are unable to transform their input space
- Feature construction does not add to the cost of acquiring original features – it only carries computational cost
- Often, feature construction can lead to dimensionality reduction or implicit feature selection

Feature Construction

- A kind of feature transformation to produce high-level constructed features that discover the relationships between features and augment the feature space
- Given $(X_1, X_2, . . . , X_m)$ - the vector corresponding to the set of original features, a constructed feature is a scalar function φ that transforms the set to a one-dimensional space: $\varphi\ (X_1, X_2, . . . , X_m)$

Example: Give $[X_1, X_2, X_3]$,
linear construction: $Xc=X_1+X_2$, $Xc=4X_1+3X_2+6X_3$, …
nonlinear construction: $Xc=X_1{*}X_2$, $Xc=X_2{*}X_3^2$, …
…

Feature Construction Process



Construct New Features - Operators

The choice of operators/functions is based on domain knowledge and the type of features

- Boolean features: Conjunctions, Disjunctions, Negation
- Nominal features: Cartesian product, M of N etc.
- Numerical features: Min, Max, Addition, Subtraction, Multiplication, Division, Average, Equivalence, Inequality etc.

A major challenge in feature construction: choosing the right set of operators and applying them appropriately

- Search space in feature construction is the space of possible functions of input features
  - How big is it?

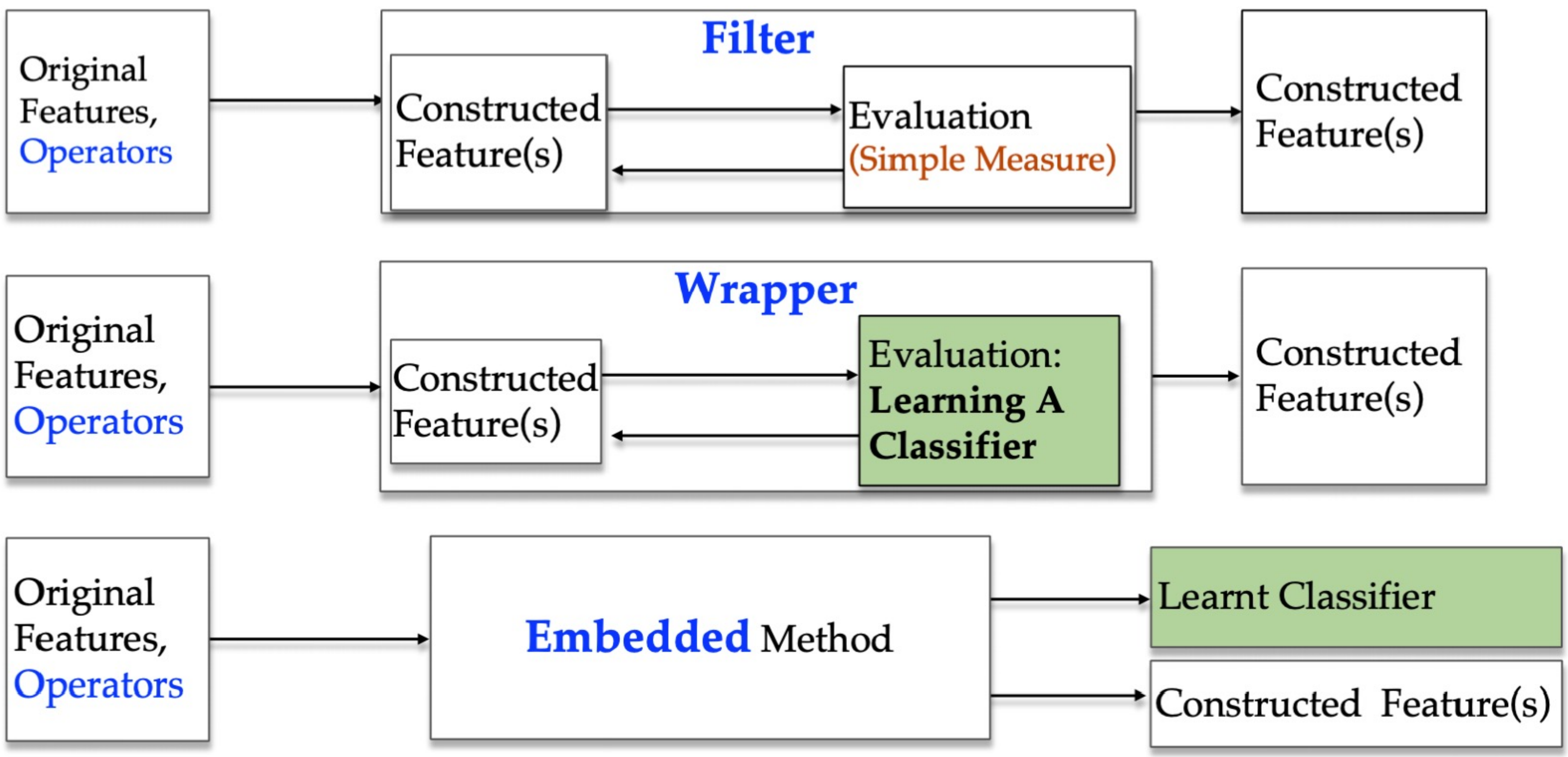
Evaluate and Select New Features

- Not all constructed features are good
- Apply feature selection techniques to remove redundant and irrelevant features
- Require an effective measure to evaluate the new features and provide an indicator
- Not computationally expensive
- Measures of consistency, distance, learning performance

Feature Construction Methods

Based on Evaluation ——— learning algorithm

- Three categories: Filter, Wrapper, Embedded
- Hybrid (Combined)



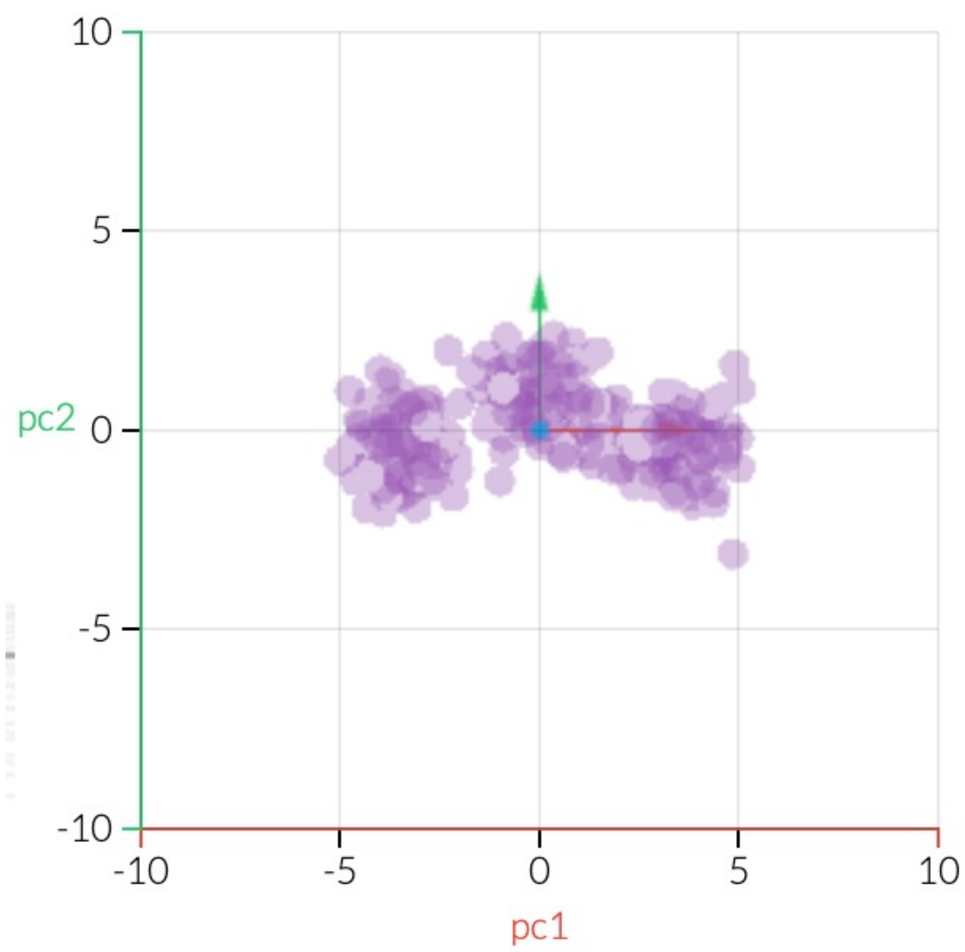
Feature Construction Methods

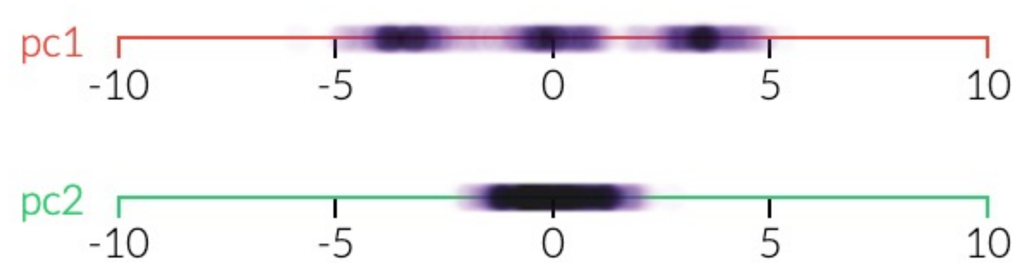
- Comparing the three categories:

	Classification Accuracy	Computational Cost	Generality (to different classifiers)
Filter	Low	Low	High
Embedded	Medium	Medium	Medium
Wrapper	High	High	Low

Principal Component Analysis (PCA)

- Invented by Karl Pearson (1901)
- *PCA* is a mathematical procedure that ***linearly*** transforms *(possibly) correlated* features into a (*smaller*) number of *uncorrelated* features called *principal components*.
- Goal is to achieve *high data variance*





Principal Components

From P original features: $x_1, x_2, \ldots, x_p$:

Produce K new features: $y_1, y_2, \ldots, y_k$:

$$
\left.
\begin{aligned}
y_1 &= a_{11}x_1 + a_{12}x_2 + \ldots + a_{1p}x_p \\
y_2 &= a_{21}x_1 + a_{22}x_2 + \ldots + a_{2p}x_p \\
&\ldots \\
y_k &= a_{k1}x_1 + a_{k2}x_2 + \ldots + a_{kp}x_p
\end{aligned}
\right\}
$$

y_k's are Principal Components

y_k's are uncorrelated (orthogonal)

- At most P principal components can be built
- Rank principal components based on their explained variance ratio then select K top-ranked ones
- How to set K?

Independent Component Analysis (ICA)

- Formally introduced by Pierre Comon in 1994

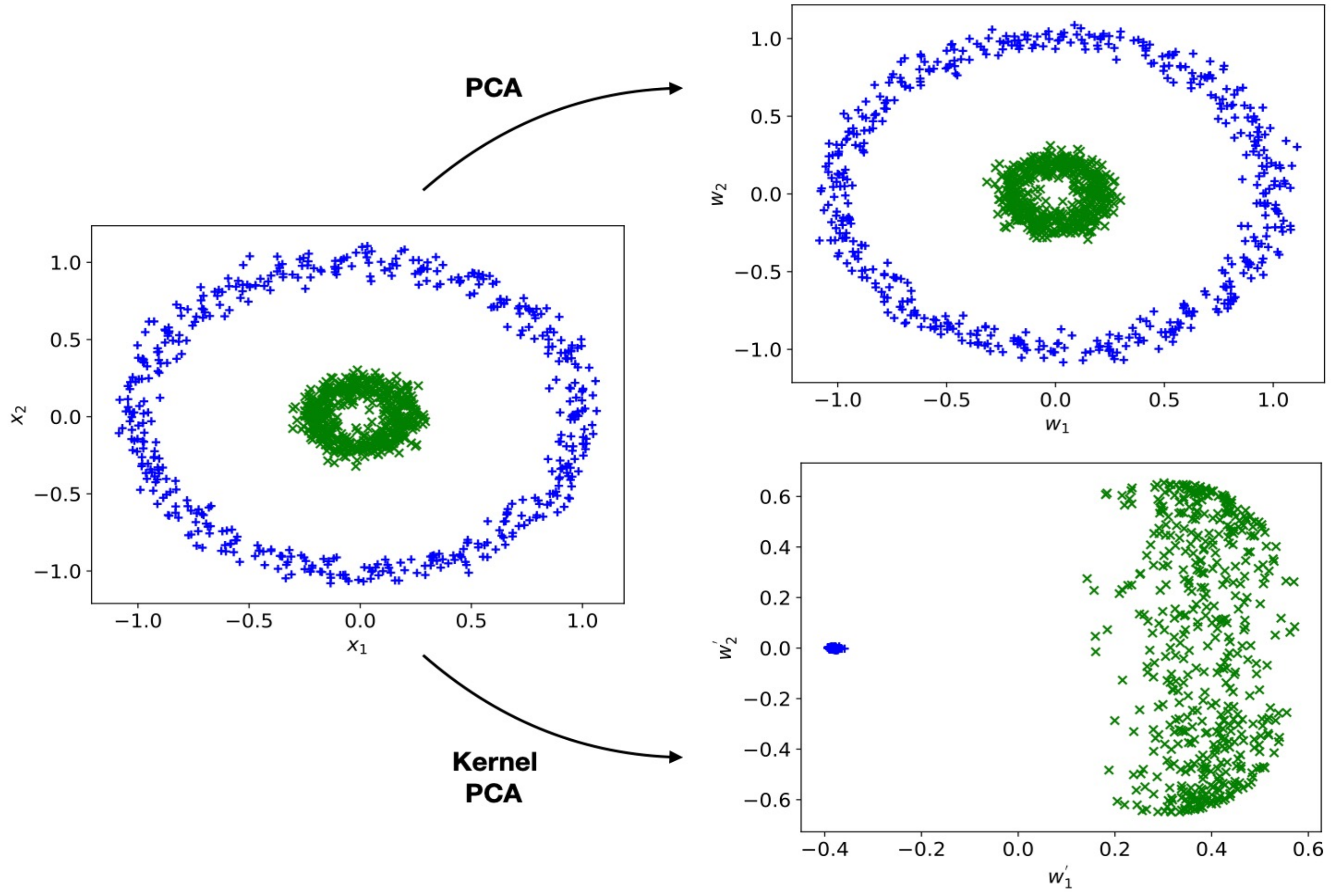
- Like PCA, ICA creates new components that are linear combinations of the original variables
- Components are as **statistically independent**

$$p(x, y) = p(x)p(y)$$

- Searching for independent components by
  - Maximising the non-Gaussianity: more than just correlation
  - Minimising the statistical independence between new components

Kernel Principal Component Analysis

- Kernel PCA combines a specific mathematical view of PCA with kernel functions, nonlinear extension of PCA
- Perform PCA on the transformed data $\Phi(x)$- "blessing of dimensionality"
- Φ - Radial basis function kernel (RBF), Polynomial function, …



https://ml-lectures.org/docs/structuring_data/ml_without_neural_network-2.html

Polynomial Features

- Polynomial features are created by raising existing features to an exponent.
- Generate a new feature matrix with the polynomial combinations of the features with a degree (less than or equal to the specified degree)

Example: Two-dimensional input feature space $[x_1, x_2]$
the ***degree-2*** polynomial features: $[1, x_1, x_2, x_1^2, x_1x_2, x_2^2]$

- Higher degree leads to larger number of features -> consider feature selection
- Change the probability distribution of features by separating the small and large values
- Appropriate degree can improve ML algorithms typically linear algorithms

GP For Feature Construction (Bonus)

- Genetic Programming is flexible in making mathematical and logical functions
- There isn't much structural (topological) information in the search space of possible functions, so using a meta-heuristic approach (such as evolutionary computation) seems reasonable