

### Possibly useful formulae

For a discrete random variable

$$E(X) = \sum_{\text{all } x} xP(X = x),$$
$$E(X^2) = \sum_{\text{all } x} x^2P(X = x),$$
$$E(g(X)) = \sum_{\text{all } x} g(x)P(X = x).$$

For a continuous random variable

$$E(X) = \int_{-\infty}^{\infty} xf_X(x)dx$$
$$E(X^2) = \int_{-\infty}^{\infty} x^2f_X(x)dx,$$
$$E(g(X)) = \int_{-\infty}^{\infty} g(x)f_X(x)dx.$$

For any random variable

$$\text{Var}(X) = E(X^2) - [E(X)]^2$$

For a binomial random variable with parameters  $n$  and  $p$ :

$$E(X) = np, \quad \text{Var}(X) = np(1-p), \quad P(X = k) = \binom{n}{k} p^k(1-p)^{n-k}, \quad k = 0, 1, 2, \dots, n$$

For a geometric random variable with parameter  $p$ :

$$E(X) = \frac{1}{p}, \quad \text{Var}(X) = \frac{1-p}{p^2}, \quad P(X = k) = (1-p)^{k-1}p, \quad k = 1, 2, 3, \dots$$

For a Poisson random variable with parameter  $\lambda$ :

$$E(X) = \lambda, \quad \text{Var}(X) = \lambda, \quad P(X = k) = e^{-\lambda} \frac{\lambda^k}{k!}, \quad k = 0, 1, 2, \dots$$

A 95% confidence interval for a parameter has the form:  
point estimate  $\pm 1.96 \times se(\text{point estimate})$

A 90% confidence interval for a parameter has the form:  
point estimate  $\pm 1.645 \times se(\text{point estimate})$

where point estimate is the estimate of the parameter and  $se(\cdot)$  is the standard error of the point estimate.