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# Big-O and sorting

# Insert sort

```
List<Integer> result = new ArrayList<Integer>();
```

```
//Insert all numbers into the result collection at the
```

```
for(int num : numbers) {
```

n

```
//Loop until end of the result loop, or the pos whe
```

```
for (int i = 0; i <= result.size(); i++) {
```

n\*n

```
if(i== result.size() || result.get(i) > num) {
```

n\*n

```
    //Insert num at this position
```

```
    result.add(i, num);
```

n..n\*n

```
    break;
```

```
}
```

```
}
```

Therefore  $O(n^2)$

```
}
```

# Bubble sort: $O(n^2)$

```
List<Integer> result = new ArrayList<Integer>(numbers);
```

```
//Move high values toward the end
```

```
for(int i = 0; i<result.size()-1; i++) {
```

n times

```
    //Swap incorrectly positioned values
```

```
    if(result.get(i) > result.get(i+1)) {
```

n

```
        Collections.swap(result, i, i+1);
```

1..n

```
        //Restart at beginning of the collection
```

```
        i = -1; //i++ happens after this so will become
```

1..n

```
    }
```

$O(n)$ ? WRONG!

```
}
```

# Bubble sort: $O(n^2)$

```

List<Integer> result = new ArrayList<Integer>(numbers);

//Move high values toward the end
for(int i = 0; i<result.size()-1; i++) {
    //Swap incorrectly positioned values
    if(result.get(i) > result.get(i+1)) {
        Collections.swap(result,i,i+1);

        //Restart at beginning of the collection
        i = -1; //i++ happens after this so will become
    }
}

```

$n*(1..n)$  times

$n*(1..n)$

$1..n$

$1..n$

$O(n^2)$

# Bogo sort

---

```
List<Integer> result = new ArrayList<Integer>(numbers);  
  
//Shuffle collection and check if it is sorted  
while(!isSorted(result)) {  
    Collections.shuffle(result);  
}
```

How  
Pro  
so average case is  $O((n+1)!)$ , worst case  $O(\text{infinite})$ , best case  $O(n)$

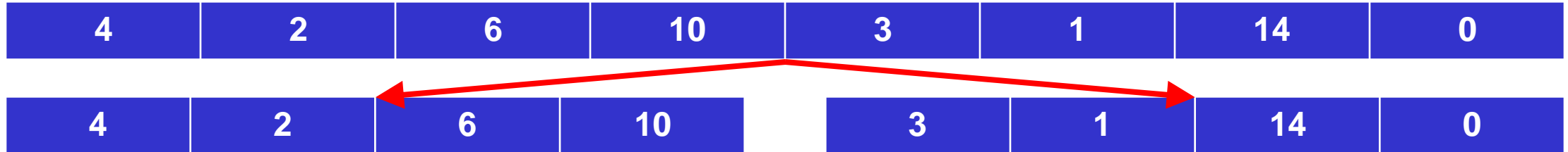
# Merge sort:

---

4	2	6	10	3	1	14	0
---	---	---	----	---	---	----	---

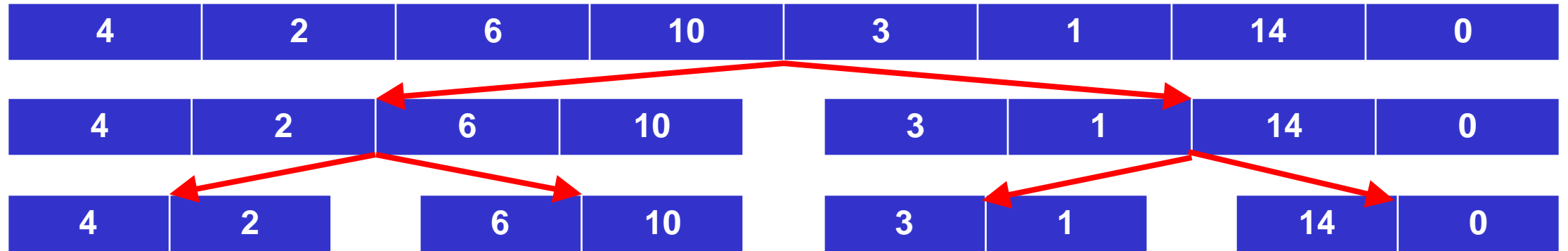
# Merge sort: Split recursively

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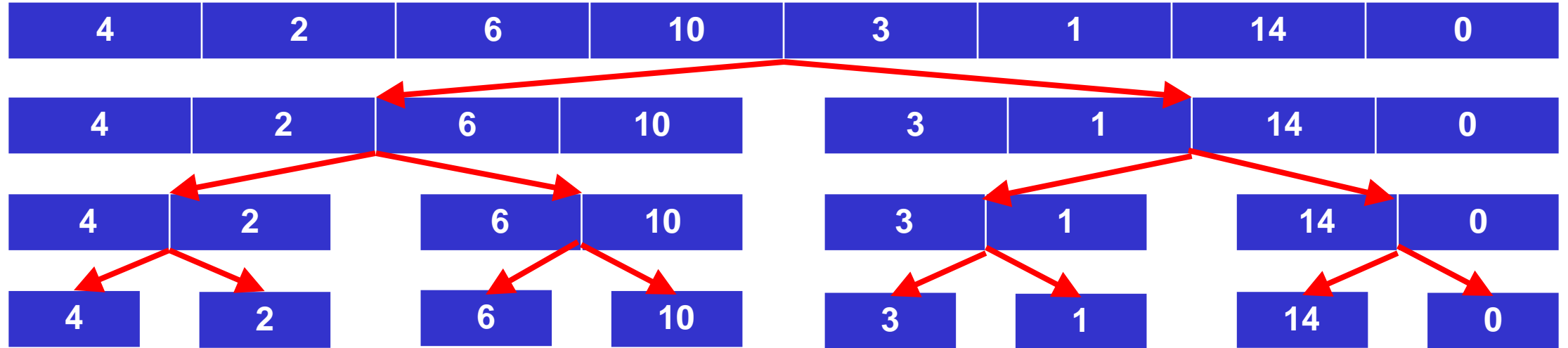
# Merge sort: Split recursively

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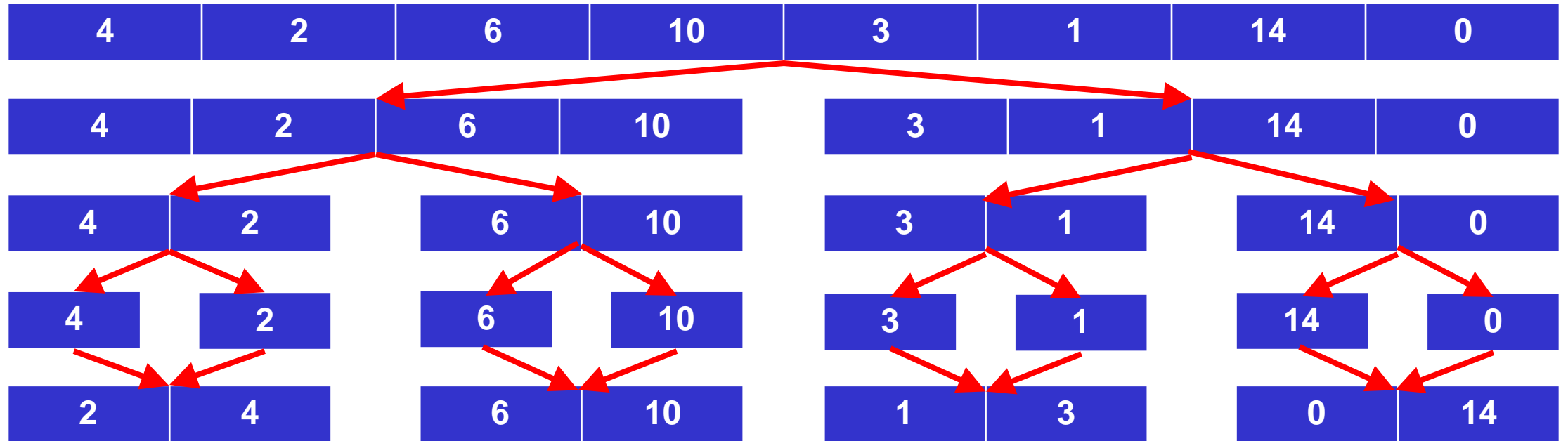




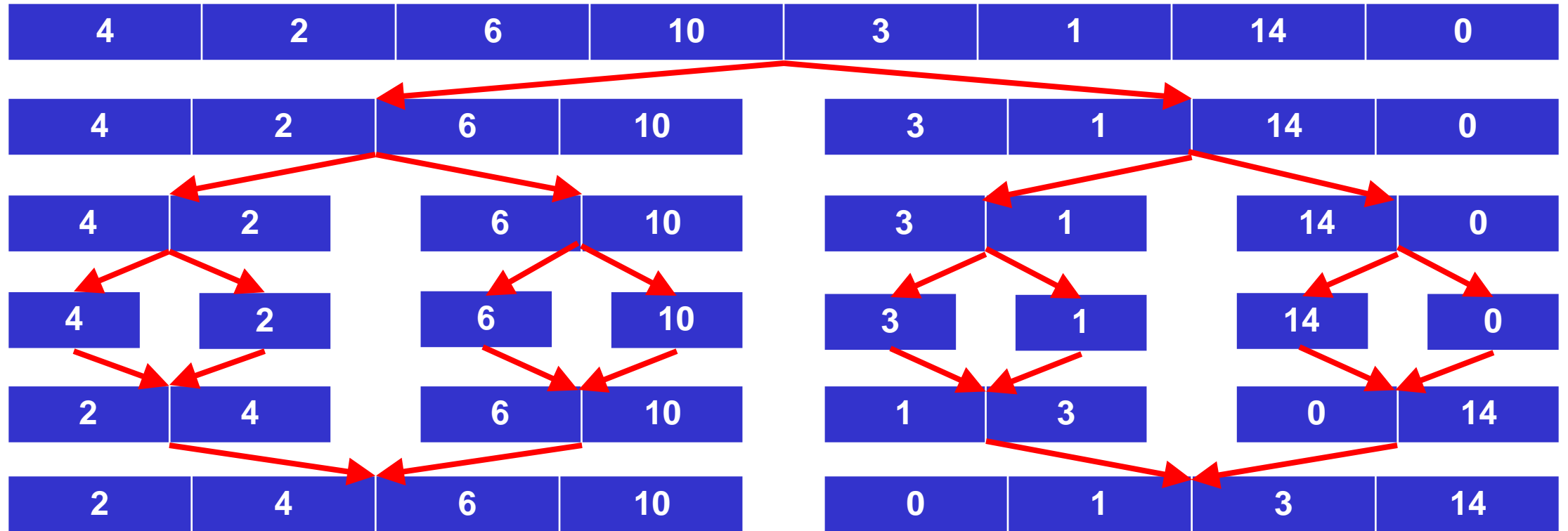
# Merge sort: Split recursively



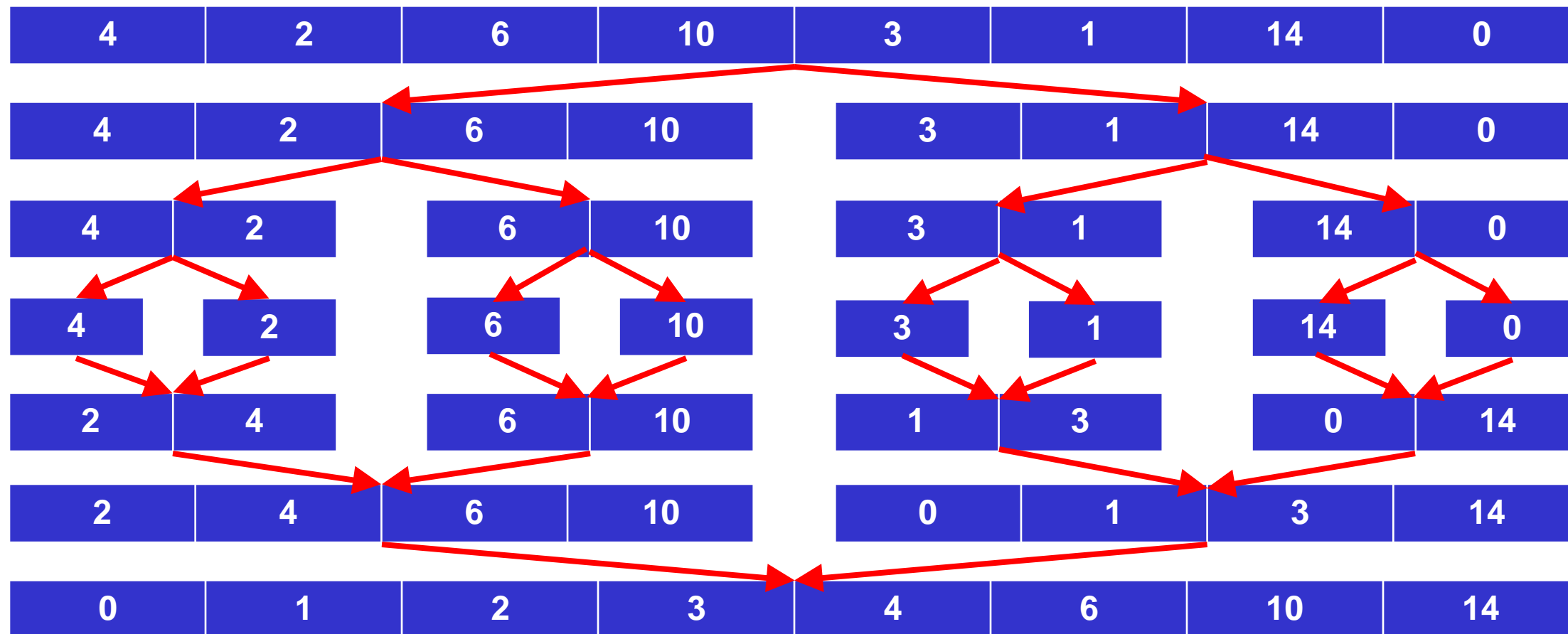
# Merge sort: Split recursively



# Merge sort: Merge recursively



# Merge sort: Merge recursively



# Merge sort: $O(n \cdot \log n)$

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List of length  $n$

Recursively divide into two halves until length 0 or 1:

$\log(n)$  layers

Recursively split:

Java 7+:  $O(1)$  at each layer

Java 1-6 :  $O(n)$  at each layer

Recursively merge the lists together in each layer:

$n$  comparisons at each “level”

Java 7+:  $0.5 \cdot \log(n) \cdot n$

Java 1-6:  $n \cdot \log(n)$