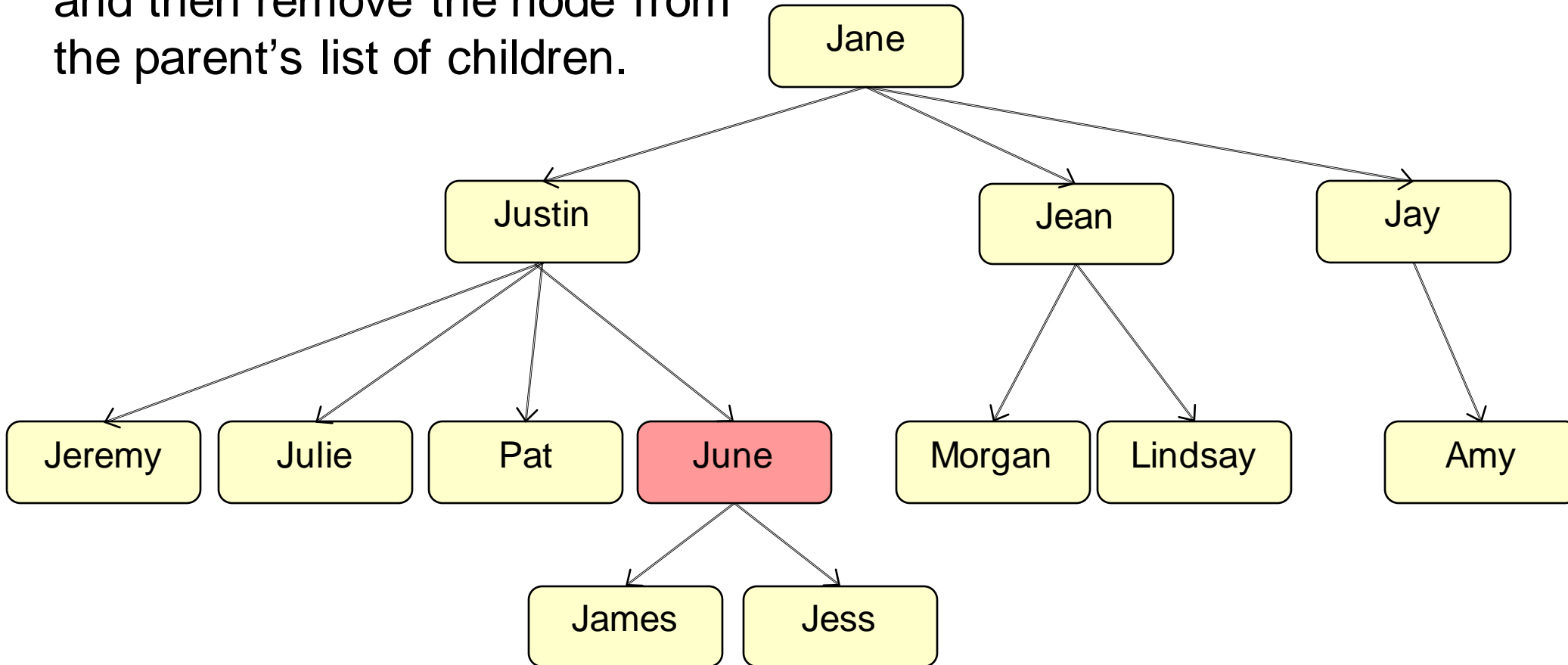


Removing a node from a Tree

- If you find a node, how do you remove it?
- Have to find the node's parent, and then remove the node from the parent's list of children.



Removing a node (and subtree) from a Tree

- Depth first traversal with “look ahead”

```
public void removePerson(Person tree, String name){  
    if (tree == null) { return; }  
    for (Person child : tree.getChildren()){  
        if (child.getName().equals(name)) {  
            tree.removeChild(child);  
            return;  
        }  
        else {  
            removePerson(child, name);  
        }  
    }  
}
```

How many nodes might it remove?

What if the person to remove is at the root of the tree

Not allowed to remove child from inside the foreach loop!!

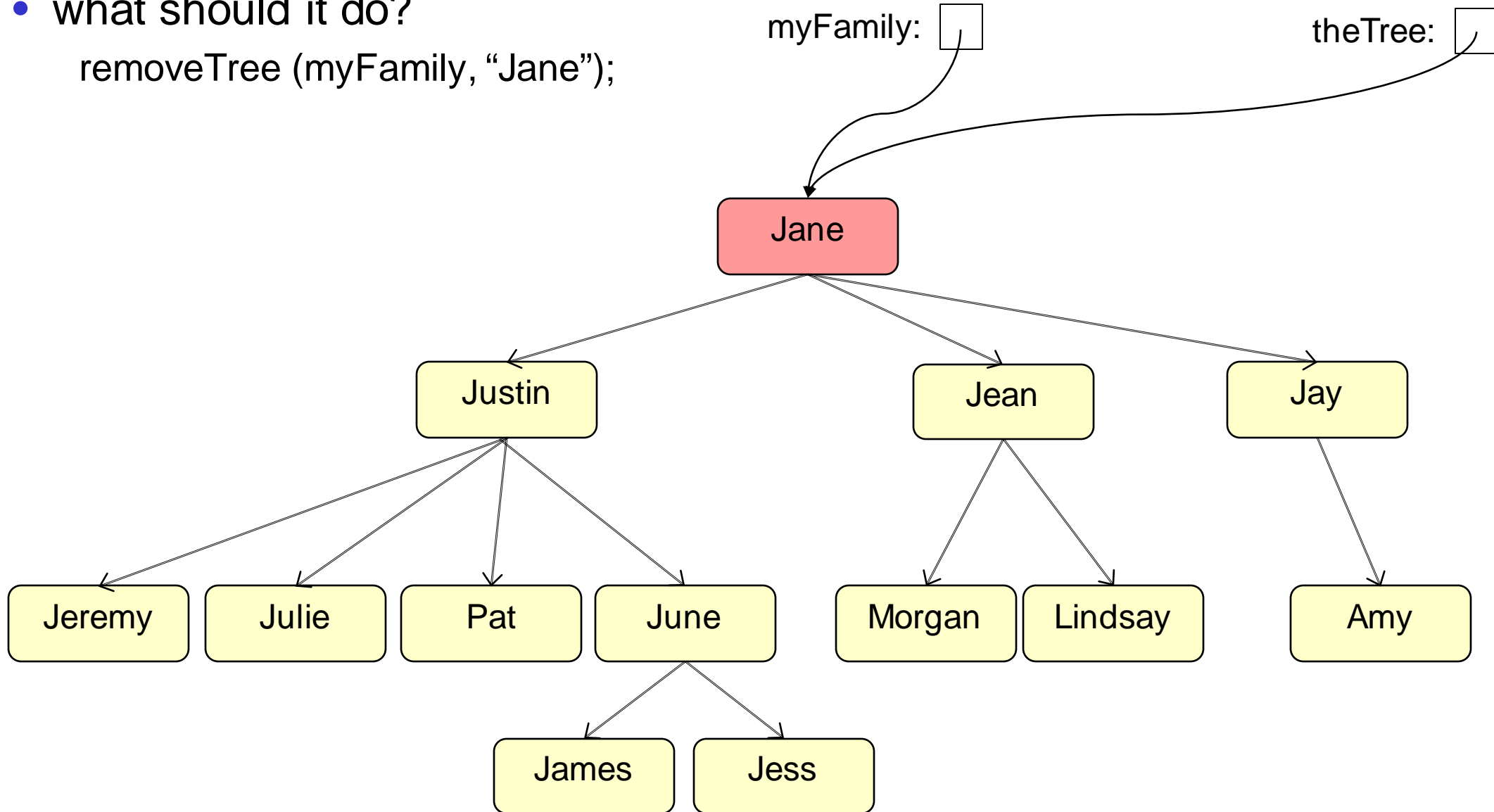
Removing a node (and subtree) from a Tree

- DF traversal, “look ahead”, remove after loop, return success when removed

```
public boolean removePerson(Person tree, String name){
    if (tree == null){ return false; }
    Person chToRemove = null;
    for (Person ch : tree.getChildren()){
        if (ch.getItem().equals(target)){ chToRemove = ch; break; }
        else {
            if (removeNode(ch, target)) { return true; }
        }
    }
    if (chToRemove==null){ return false; }
    tree.removeChild(chToRemove);
    return true;
}
```

Removing the root node from a Tree

- what should it do?
`removeTree (myFamily, "Jane");`



General Trees with parent links

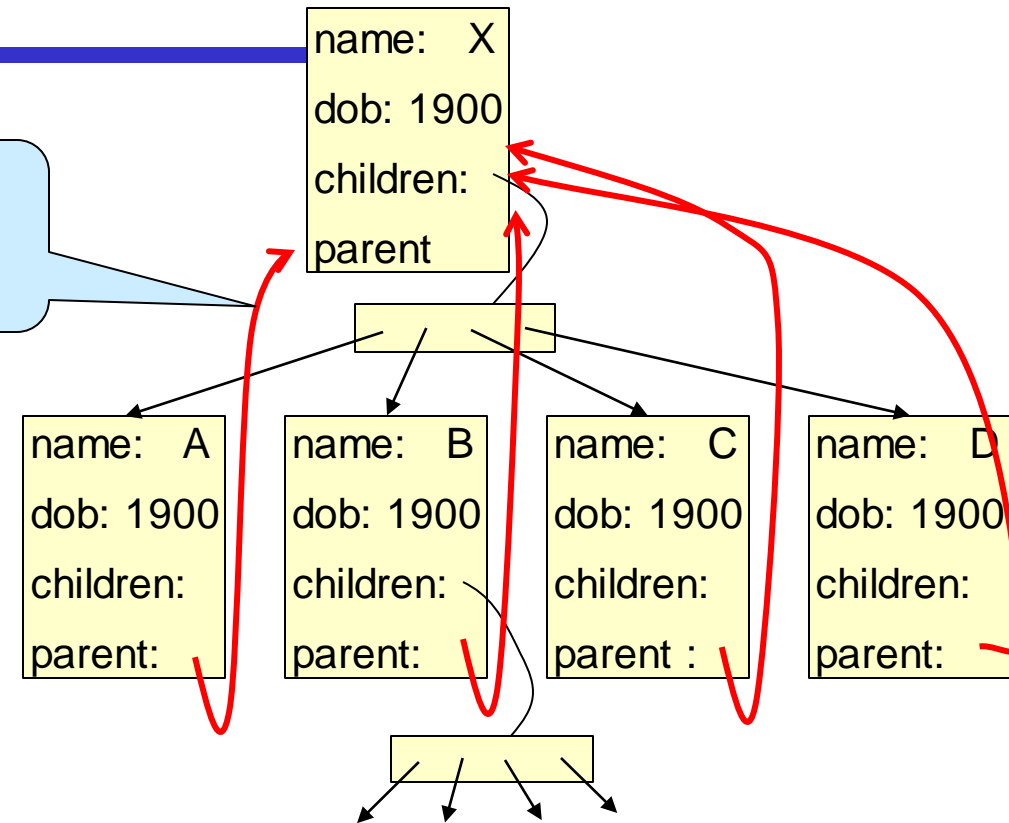
```
public class Person {
    private String name;
    private int dob;
    private Set<Person> children;
    private Person parent;
```

```
    :
    public Person getParent(){ return parent; }
    public void setParent(Person p){parent = p; }
```

```
    public Person getChildren(){ return Collections.unmodifiableSet(children);}
    public void addChild(Person ch){ children.add(ch); }
    public void removeChild(Person ch){ children.remove(ch); }
```

```
}
```

Parent links make it easy to get the parent of a node

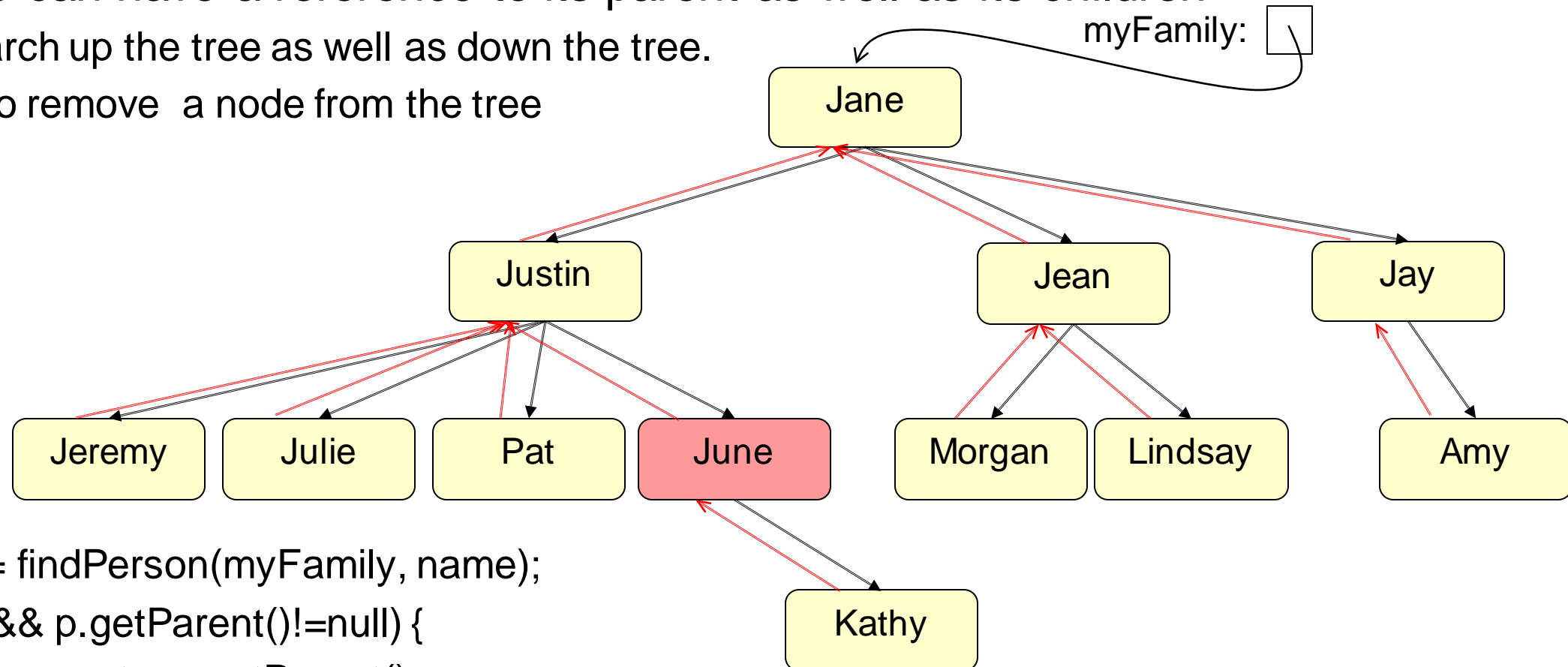


General Trees with parent links

- Each node can have a reference to its parent as well as its children

⇒ can search up the tree as well as down the tree.

⇒ easier to remove a node from the tree



```
Person p = findPerson(myFamily, name);
```

```
if (p!=null && p.getParent()!=null) {
```

```
    Person parent = p.getParent();
```

```
    parent.removeChild(p);
```

```
    p.setParent(null);
```

```
}
```

Following parent links: OrganisationChart

To determine horizontal placement of Position node:

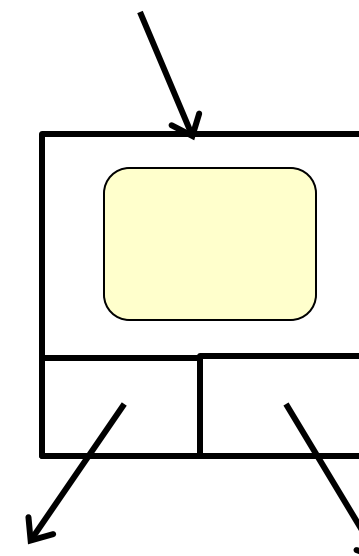
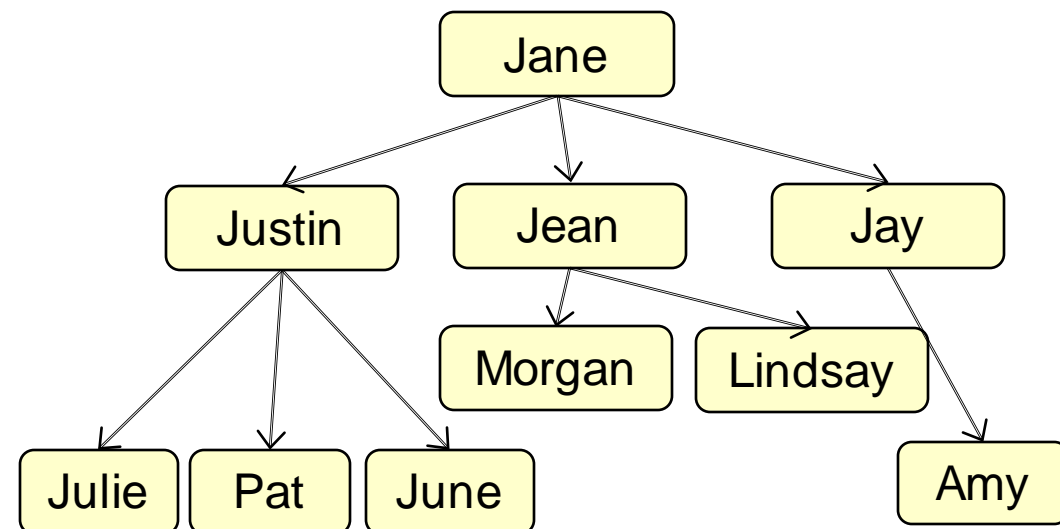
- Position contains horizontal **offset** from parent (manager)
Must find parent's position and then add the offset:

(in Position class)

```
public int getX(){
    if (this.manager==null) { // this is the root of the tree.
        return BASE_X + this.offset;
    }
    else { // relative to position of parent.
        return this.manager.getX() + this.offset;
    }
}
```

Trees of Data vs Trees containing Data

- Person, Position, ...
 - The data object contains the links that make the tree.
 - Person: father, mother, children, ...
 - Employee: manager, team
- Typical Collection (Set, Map, Queue...)
 - The collection has the structure,
 - The data objects sit inside the structure
- Tree data structures:
 - Node object that has fields for the data item, and for the links.



Tree Node types

- There is no single way of defining tree structures

- Need to make your own.

eg: Binary tree node:

```
public class BTNode <E> {
    private E item;
    private BTNode<E> left;
    private BTNode<E> right;

    public BTNode(E item) { this.item = item; }

    public E getItem()          { return item; }
    public void setItem(E item) { this.item = item; }

    public BTNode<E> getLeft()   { return left; }
    public void setLeft(BTNode<E> left) { this.left = left; }

    public BTNode<E> getRight()  { return right; }
    public void setRight(BTNode<E> right) { this.right = right; }
}
```

Type variable: parameter of the ***type***
specify when you make a new node:

Using BTreeNode: Expressions

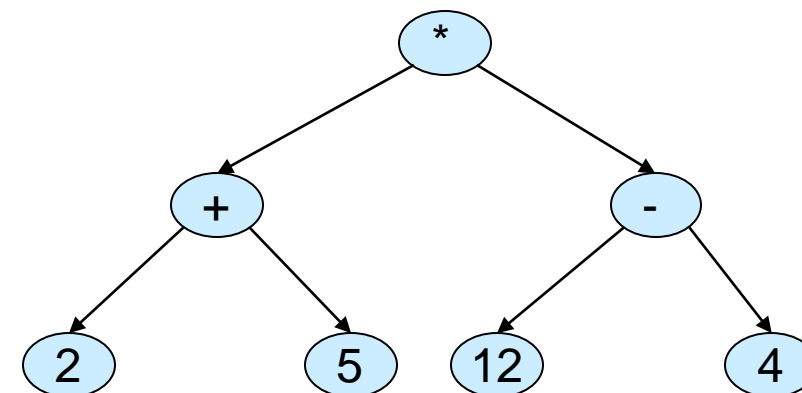
- $(2 + 5) * (12 - 4)$

- Printing:

- standard format with (...)
- pre-order: $* + 2 5 - 12 4$
- post-order: $2 5 + 12 4 - *$

“Polish notation” -
never need brackets!

“Reverse Polish notation”



- Evaluating

- recursive, post-order traversal of tree

- Reading

- pre-order and post-order: easy
- in order: hard! (COMP 261, simple parsing algorithms)

Same tree, different print format.

- Polish and Reverse Polish are easier to parse
- Require fewer keystrokes on a calculator.
- Reverse Polish can be evaluated while reading

Cambridge Polish notation

- Expressions with operators with variable number of arguments
- => general tree.

- Writing such expressions:

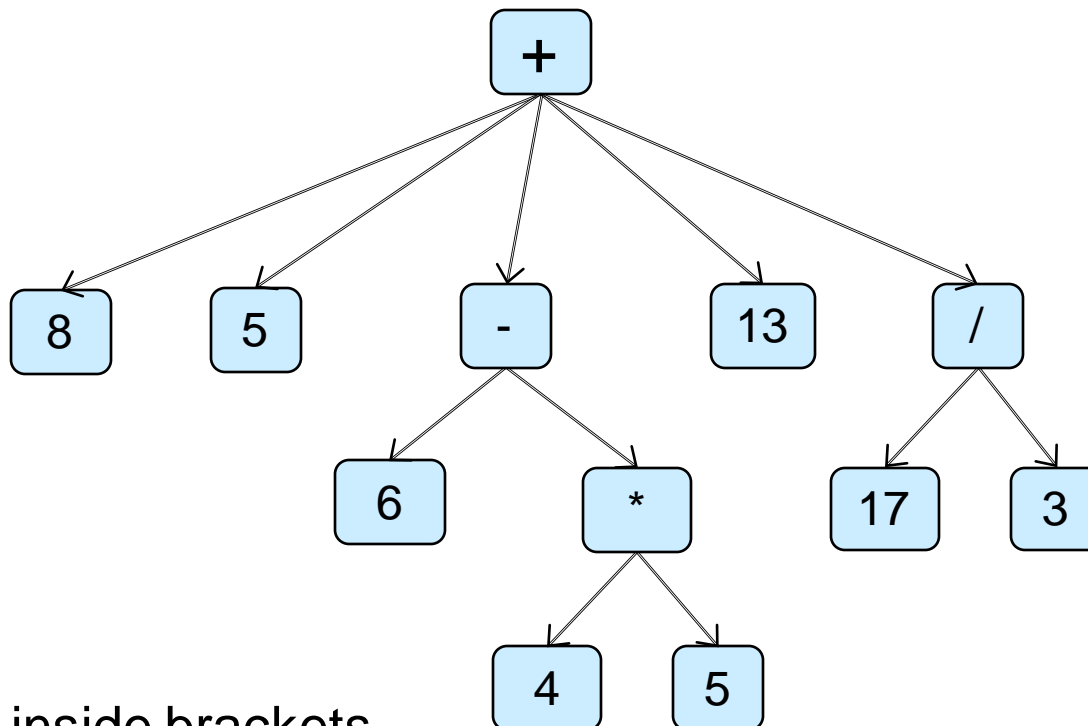
- Normal functional notation:
Pre-order, with brackets and commas
operator before brackets

eg: $+(8, 5, -(6, *(4, 5)), 13, /(17\ 3))$

- Cambridge Polish Notation (Lisp)
Pre-order, in brackets, no commas, operators inside brackets

eg: $(+ 8 5 (- 6 (* 4 5)) 13 (/ 17 3))$

- Assignment: Make a calculator for this:
 - read (given), evaluate, print (REPL)



Same tree, different print format.
CPN is easier to parse

General Tree Nodes.

```
public class GTNode <E> {
    private E item;
    private List<GTNode<E>> children;           // List, therefore children kept in order.
```

```
/** Constructor for objects of class GTNode */
public GTNode(E item){
    this.item = item;
    this.children = new ArrayList<GTNode<E>>();
}
/** Getters and Setters */
public E getItem()           { return item; }
public void setItem(E item) { this.item = item; }
```

- What about the children?

```
public List<GTNode<E>> getChildren() { return Collections.unmodifiableList(children; }
```

Good design:
Protect the inner structure of the objects from modification by the rest of the program!

General Tree Node: Alternative design

- Keep the List of children internal to the class.
- Provide methods to add and remove children

```
/** Getters and Setters */
```

```
public GTNode<E> getChild(int indx) { return children.get(indx); }
```

```
public void addChild(GTNode<E> child) { this.children.add(child); }
```

```
public void addChild(int indx, GTNode<E> child) { this.children.set(indx, child); }
```

```
public void setChild(int indx, GTNode<E> child) { this.children.set(indx, child); }
```

- What about iterating through the children?

- Could return child node at given index:

```
public GTNode<E> getChild(int indx) { return this.children.get(indx); }
```

- Could enable foreach loop:

```
for (GTNode<String> child : node) { .... }
```

HOW?

Iterable and Iterators

- To be able to iterate along an object using foreach loop, the object must be **Iterable**:
- The object's class must implement `Iterable<??>` and have a **public Iterator<??> iterator(){...}** method which returns an Iterator object
- An Iterator object must have a **public boolean hasNext() {...}** method, and a **public ??? next() {...}** method

General Tree Nodes.

```

public class GTNode <E> implements Iterable <GTNode<E>> {
    private E item;
    private List<GTNode<E>> children;           // List, therefore children kept in order.

    /**Constructor for objects of class GTNode */
    public GTNode(E item){
        this.item = item;
        this.children = new ArrayList<GTNode<E>>();
    }
    /** Getters and Setters */
    public E getItem()           { return item; }
    public void setItem(E item) { this.item = item; }

    public Iterator<GTNode<E>> iterator() { return children.iterator(); }

```

Using GTNode with iterator

- look for a node in a tree with a particular item (recursive depth-first traversal)

```
public GTNode<String> findNode(GTNode<String> root, String label){
    if (root.getItem().equals(label) ) {
        return root;
    }
    for (GTNode<String> child : root) {
        GTNode<String> ans = findNode(child, label);
        if (ans != null) {
            return ans;
        }
    }
    return null;
}
```