

XMUT310 Communication Engineering

Tutorial 2: Amplitude Modulation (AM)

Answers are provided for your convenience.

Most solutions can be found on Bilibili <https://www.bilibili.com/video/BV1Yy4y1z79x> and <https://www.bilibili.com/video/BV12p4y167BP/> and <https://www.bilibili.com/video/BV1kt4y1e7r3>

Q1. A modulating signal of frequency 5 kHz and peak voltage of 6 V is used to modulate a carrier of frequency 10 MHz and peak voltage of 10 V. Determine (a) Modulation index, (b) Frequency of LSB and USB, (c) Amplitude of LSB and USB.

(Answers: (a) 60%, (b) 9.995 MHz and 10.005 MHz, (c) 3 V)

Q2. For an amplitude modulated wave, the maximum amplitude is found to be 10 V while the minimum amplitude is found to be 6 V. Determine the modulation index (%) and amplitude of original carrier frequency.

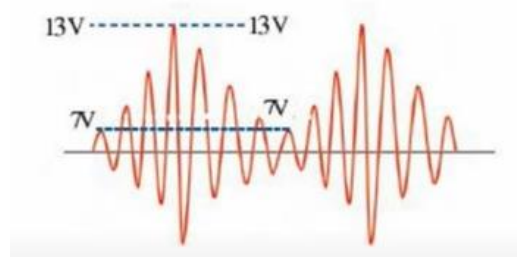
(Answers: 25%, 8V)

Q3. If the frequency of 3 kHz signal is to be transmitted through amplitude modulation, which of the following frequency should be used as a carrier frequency?

- a. 30 Hz
- b. 300 Hz
- c. 3000 Hz
- d. 3 MHz

(Answer: d)

Q4. What will be the modulation index of the following AM wave?



- a. 6%
- b. 20%
- c. 30%
- d. 50%

(Answer: c)

Q5. A carrier wave of 2 MHz is amplitude modulated by a modulating wave of 2 kHz. Which of the following frequencies will be present in the AM wave?

- a. 2 MHz, 2 kHz
- b. 2 kHz, 2.002 MHz, 1.998 MHz

- c. 2 MHz, 2.002 MHz, 1.998 MHz
- d. 2.002 MHz, 1.998 MHz

(Answer: c)

Q6. The maximum amplitude of carrier wave is 12 V. What should be the amplitude of modulating signal in order to have a modulation index of 75%?

(Answer: 9 V)

Q7. The equation of AM wave is given as $x(t) = 100(1 + 0.6\sin 6280t)\sin(2\pi \times 10^6t)$. Calculate (a) modulation index, (b) frequency of carrier wave, (c) frequency of modulating wave, (d) frequency of LSB and USB.

(Answers: (a) 60%, (b) 1 MHz, (c) 1 kHz, (d) 0.999 MHz and 1.001 MHz)

Q8. Find the total modulated power, side power and net modulation index for the AM signal expressed in volts, $y(t) = 10\cos(2\pi \times 10^6t) + 5\cos(2\pi \times 10^6t)\cos(2\pi \times 10^3t) + 2\cos(2\pi \times 10^6t)\cos(4\pi \times 10^3t)$.

(Answer: total power = 57.25 W, side power = 7.25 W, modulation index = 53.9%)

Q9. An amplitude modulated amplifier has radio frequency output of 50 W at 100% modulation index with internal loss in modulator of 10 W.

- a. What is the unwanted carrier power?
- b. What power output is required from the sideband (baseband signal)?
- c. If the percentage modulation is reduced to 75%, how much output is needed from the sideband (baseband signal), assuming that the total transmitted power remains the same?

(Answers: (a) 40 W, (b) 20 W, (c) 13.18 W)

Q10. The modulation index of an AM wave is changed from 0 to 1. The transmitted power is

- a. Unchanged
- b. Halved
- c. Increased by 50%
- d. Quadrupled

(Answer: c)

Q11. An AM wave is given by $y(t) = 10[1 + 0.4\cos(10^3t) + 0.3\cos(10^4t)]\cos(2\pi \times 10^6t)$. The modulation index of the envelope is

- a. 0.4
- b. 0.5
- c. 0.3
- d. 0.9

(Answer: b)

Q12. The most suitable method for detecting a modulated signal $[2.5 + 5\cos(w_mt)]\cos(w_ct)$ is

- a. Envelope detector
- b. Synchronous detector
- c. Radio detector
- d. Both a and b

(Answer: b)

Q13. Prove that for an AM, the maximum average power transmitted by AM is 1.5 times the carrier power.

Q14. The antenna current of an AM broadcast transmitter, modulated to a depth of 40% by an audio sine wave is 11 amp. It increases to 12 amp as a result of simultaneous modulation by another audio sine wave. Find the modulation index due to this second sine wave.

(Answer: 64.3%)

Q15. Determine the efficiency and the percentage of the total power carried by sinusoids of AM wave for tone modulation when $\mu = 1, 0.5$ and 0.3 .

(Answers: (a) when $\mu = 1$, efficiency and side power = 33.33%, (b) when $\mu = 0.5$, 11.11%, (c) when $\mu = 0.3$, 4.3%)

Q16. Calculate the percentage of power saving by DSB-SC for a modulating index of (a) 100% (b) 50%.

(Answers: (a) 66.67%, (b) 88.88%)

Q17. Calculate the percentage of power saving by SSB for a modulating index of (a) 100% (b) 50%.

(Answers: (a) 83.33%, (b) 94.44%)

Q18. A message signal $m(t) = \cos 2000\pi t + 4\cos 4000\pi t$ modulates the carrier $c(t) = \cos 2\pi f_c t$ where $f_c = 1$ MHz to produce an AM signal. For demodulating the generated AM signal using an envelope detector, the time constant RC of the detector circuit should satisfy

- a. $0.5 \text{ ms} < RC < 1 \text{ ms}$
- b. $1 \text{ us} < RC < 0.5 \text{ ms}$
- c. $RC < 1 \text{ us}$
- d. $RC > 0.5 \text{ ms}$

(Answer: b)

Q19. Suppose that the modulating signal is $m(t) = 2\cos(2\pi f_m t)$ and the carrier signal is $x_c(t) = A_c \cos(2\pi f_c t)$, which one of the following is a conventional AM signal without over-modulation?

- a. $x(t) = A_c m(t) \cos(2\pi f_c t)$
- b. $x(t) = A_c [1 + m(t)] \cos(2\pi f_c t)$
- c. $x(t) = A_c \cos(2\pi f_c t) + A_c/4 m(t) \cos(2\pi f_c t)$
- d. $x(t) = A_c \cos(2\pi f_c t) \cos(2\pi f_m t) + A_c \sin(2\pi f_c t) \sin(2\pi f_m t)$

(Answer: c)

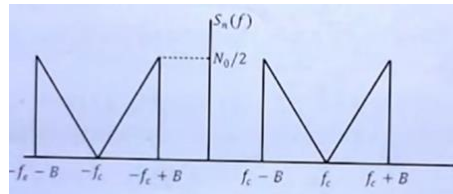
Q20. Consider the following AM signal shown here, where $f_m < B$, $x_{AM}(t) = 10(1 + 0.5\sin 2\pi f_m t) \cos 2\pi f_c t$. The average side-band power in W for the AM signal given above is

- a. 25

- b. 12.5
- c. 6.25
- d. 3.125

(Answer: c)

Q21. The AM signal in Q20 gets added to a noise with power spectral density $S_n(f)$ given in the figure below. The ratio of average sideband power to mean noise power would be:



- a. $25/8N_0B$
- b. $25/4N_0B$
- c. $25/2N_0B$
- d. $25/N_0B$

(Answer: b)

Q22. A 1 MHz sinusoid carrier is amplitude modulated by a symmetrical square wave of period 100 μ sec. Which of the following frequencies will NOT be present in the modulated signal?

- a. 900 kHz
- b. 1010 kHz
- c. 1020 kHz
- d. 1030 kHz

(Answer: c)

Q23. For a message $m(t) = \cos(2\pi f_m t)$ and carrier of frequency f_c , which of the following represents a single-sideband (SSB) signal?

- a. $\cos(2\pi f_m t) \cos(2\pi f_c t)$
- b. $\cos(2\pi f_c t)$
- c. $\cos[2\pi(f_c + f_m)t]$
- d. $[1 + \cos(2\pi f_m t)] \cos(2\pi f_c t)$

(Answer: c)

Q24. A message signal given by $m(t) = \frac{1}{2} \cos \omega_1 t - \frac{1}{2} \sin \omega_2 t$ is amplitude-modulated with a carrier of frequency ω_c to generate $s(t) = [1 + m(t)] \cos \omega_c t$. What is the power efficiency achieved by this modulation scheme?

- a. 8.33%
- b. 11.11%
- c. 20%
- d. 25%

(Answer: c)

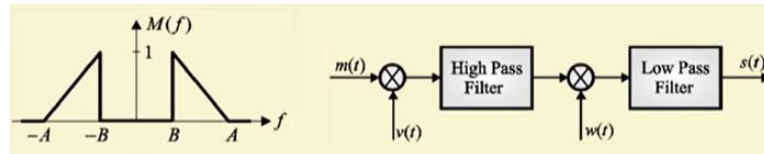
Q25. A carrier signal $c(t) = 20 \cos 2\pi 10^6 t$ is modulated by a message signal $m(t) = 20 \cos 8\pi 10^3 t$ to generate DSB-SC, calculate the bandwidth, total power and modulation efficiency.

(Answers: bandwidth = 8 kHz, total power = 100 W, efficiency = 100%)

Q26. In a DSB-SC transmission system, if the modulation index is doubled, then the ratio of total sideband power to the carrier power increases by a factor of ____?

(Answer: 4)

Q27. In the figure here, $M(f)$ is the Fourier Transform of the message signal $m(t)$ where $A = 100$ Hz and $B = 40$ Hz. Given $v(t) = \cos(2\pi f_c t)$ and $w(t) = \cos[2\pi(f_c + A)t]$ where $f_c > A$. The cut-off frequencies of both filters are f_c . The bandwidth of the signal $s(t)$ at the output of the modulator is ____ (Hz).



(Answer: 60 Hz)

Q28. Which of the following analog modulation scheme requires the minimum transmitted power and minimum channel bandwidth?

- a. VSB
- b. DSB-SC
- c. SSB
- d. AM

(Answer: c)

Q29. The Hilbert transform of $\cos w_1 t + \sin w_2 t$ is

- a. $\sin w_1 t - \cos w_2 t$
- b. $\sin w_1 t + \cos w_2 t$
- c. $\cos w_1 t - \sin w_2 t$
- d. $\sin w_1 t + \sin w_2 t$

(Answer: a)

Q30. The amplitude of a sinusoid carrier is modulated by a single sinusoid to obtain the amplitude modulated signal $s(t) = 5 \cos 1600\pi t + 20 \cos 1800\pi t + 5 \cos 2000\pi t$. The value of the modulation index is _____.

(Answer: 0.5)