



EXAMINATIONS — 2011  
**Trimester 2, MID-TERM TEST**

**COMP103**  
**Introduction to**  
**Data Structures and Algorithms**  
**SOLUTIONS**

**Time Allowed:** 45 minutes

- Instructions:**
1. Attempt **all** of the questions.
  2. *Read each question carefully before attempting it.*
  3. This test will be marked out of **45** marks, so allocate approximately one minute per mark.
  4. Write your answers in the boxes in this test paper and hand in all sheets.
  5. Documentation on some relevant Java classes, interfaces, and exceptions can be found at the end of the paper.

<b>Questions</b>	<b>Marks</b>
1. Various Questions	[10]
2. Using and Implementing Collections	[25]
3. Recursion, and Sorting	[10]

**SPARE PAGE FOR EXTRA ANSWERS**

Cross out rough working that you do not want marked.  
Specify the question number for work that you do want marked.

**Question 1. Various questions**

[10 marks]

(a) [4 marks] By drawing a circle around the correct answer, indicate whether the following statements are TRUE or FALSE:

- A Stack is an interface, that implements Collection: TRUE/FALSE False
- A Priority Queue can add elements anywhere: TRUE/FALSE True
- A for-each loop can be used on all Iterable types: TRUE/FALSE True
- Selection Sort is a stable sort: TRUE/FALSE False

(b) [2 marks] If it takes 10 steps to search through an array of 1024 items using binary search, how many steps will it take to search through an array of 4096 items (*ie.* four times as many)?

12 steps

(c) [4 marks] Write down the “Big- $\mathcal{O}$ ” costs of the following, for an array with  $n$  items:

- Insertion Sort on an almost sorted array:

Cost:  $\mathcal{O}(n)$

- Selection Sort on an almost sorted array:

Cost:  $\mathcal{O}(n^2)$

- Average case of searching for a single item in a SortedArrayBag:

Cost:  $\mathcal{O}(\log n)$

- Worst case of Merge Sort:

Cost:  $\mathcal{O}(n \log n)$

## Question 2. Using and Implementing Collections

[25 marks]

(a) [5 marks] Below is a declaration of a Map (named `todo`) which maps tasks (of type `Task`) to the name of their owners (of type `String`):

```
Map <Task, String> todo = new HashMap <Task, String> ();
```

In the box below, write the code to iterate over this map and print the tasks along with the name of their owners.

[Note: You can assume that the class `Task` is already implemented and provides a `toString()` method]

```
for (Map.Entry<Task, String> td : todo.entrySet()) {  
    UI.println ("Task = " + td.getKey() + " is owned by " + td.getValue());  
}
```

OR iterate over keys.

(b) [6 marks]

The `remove` method of a `SortedArrayBag` (similar to Assignment#4) uses the `findIndex` method to locate the item to be removed - as shown in the 3rd line, below.

Complete the `remove` method so that it removes the item and leaves the array in a correct state. It should return `true` if the collection changes, and `false` if it did not change.

```

public boolean remove (Object item) {

    if (item==null) return false;
    int index = findIndex(item);

    if (index == count || !item.equals(data[index]))
        return false;

    count--;
    for ( int i=index; i<count; i++)
        data[ i ]= data[ i +1];
    data[count]=null;
    return true;

}

```

(c) [2 marks] Explain the difference between a Bag and a Set.

Set does NOT allow duplicates, but Bag does.

(d) [2 marks] Name the collection that is used to implement “undo” operations in many applications. What property of this collection makes this possible?

collection:  
property: **FILO (first in last out) property of stack**

Consider the following CompareFaces class that stores and sorts a List of Faces, and then answer the questions on the following page.

```
public class CompareFaces{  
    private List <Face> crowd; //private field  
  
    /** constructor that instantiates a new ArrayList of Face and sorts it */  
    public CompareFaces(){  
        crowd = new ArrayList <Face>();  
        Collections.sort(crowd);  
    }  
  
    public static void main(String[] args){  
        CompareFaces cf = new CompareFaces();  
    }  
  
    :  
    :  
}
```

(e) [4 marks] For the `Collections.sort(crowd)` to work (in the constructor of the above `CompareFaces` class), the `Face` class (below) must be `Comparable`. Complete the `compareTo` method (in the `Face` class below) which compares `Faces` based on their size.

```
public class Face implements Comparable<Face>{

    private int wd;
    private int ht;
    private String name;
    private int size;

    // constructor
    public Face(String name, int w, int h, int size){
        this.name = name;
        wd = w;
        ht = h;
        this.size = size;
    }

    public int getSize(){ return size; }

    public int getPosition(){ return wd; }
    :
    :
    public int compareTo(Face other){
        // YOUR CODE HERE

        return (this.getSize()–other.getSize());

    }

} //end of Face class
```

(f) [6 marks] Write a `LeftToRightComparator` comparator that will compare `Face` objects based on their positions on the screen.

```
private class LeftToRightComparator implements ... {

private class LeftToRightComparator implements Comparator<Face>{
    public int compare(Face f1, Face f2){
        return (f1.getPosition()–f2.getPosition ());
    }
}

}
```

Question 3. Recursion and Sorting

[10 marks]

```

public void seriesRec(int n) {
    System.out.print(n + " ");
    if (n > 15)
        return;
    else
        seriesRec(3*n - 1);
}

```

(a) [4 marks] What will be printed out when seriesRec(1) is called?

1 2 5 14 41

(b) [2 marks] Given the initial array shown (1st row), identify the sorting algorithm which results in the array shown (2nd row) after 3 passes through its outer loop (assume the usual A-to-Z sort is required).

Start:	H	F	L	P	Q	E	Z
After 3 passes:	F	H	L	P	Q	E	Z

Sorting algorithm: Insertion Sort

(c) [2 marks] As with the previous question: identify the sorting algorithm which results in the following array after 3 passes through its outer loop (assume the usual A-to-Z sort is required).

Start:	M	J	B	R	P	A	D
After 3 passes:	A	B	D	R	P	M	J

Sorting algorithm: Selection Sort

(d) [2 marks]

List one advantage of MergeSort over QuickSort and one advantage of QuickSort over MergeSort.

- Advantage of MergeSort: eg. worst case still  $O(n^2)$ , is stable,...
- Advantage of QuickSort: eg. is in-place,...

\*\*\*\*\*



## Appendix (may be removed)

**Brief (and simplified) specifications of some relevant interfaces and classes.**

**public class** *Scanner*

```
public boolean hasNext(); // there is more to read
public String next(); // return the next token (word)
public String nextLine(); // return the next line
public int nextInt (); // return the next integer
```

**public class** *Random*

```
public int nextInt(int n); // return a random integer between 0 and n-1
public double nextDouble(); // return a random double between 0.0 and 1.0
```

**public interface** *Iterator* <*E*>

```
public boolean hasNext();
public E next();
public void remove();
```

**public interface** *Iterable* <*E*>

```
public Iterator <E> iterator();
```

// Can use in the "for each" loop

**public interface** *Comparable* <*E*>

```
public int compareTo(E o);
```

// Can compare this to another *E*

**public interface** *Comparator* <*E*>

```
public int compare(E o1, E o2);
```

// Can use this to compare two *E*'s

```
public class Collections
    public void sort(List<E>, Comparator<E>)
```

```
public interface Collection<E>
    public boolean isEmpty();
    public int size ();
    public boolean add();
    public Iterator <E> iterator();
```

```
public interface List<E> extends Collection<E>
    // Implementations: ArrayList
    public E get(int index);
    public void set(int index, E element);
    public void add(E element);
    public void add(int index, E element);
    public void remove(int index);
    public void remove(Object element);
```

```
public interface Set extends Collection<E>
    // Implementations: HashSet, SortedSet, TreeSet
    public boolean contains(Object element);
    public boolean add(E element);
    public boolean remove(Object element);
```

```
public interface Queue<E> extends Collection<E>
    // Implementations: LinkedList, PriorityQueue
    public E peek (); // returns null if queue is empty
    public E poll (); // returns null if queue is empty
    public boolean offer (E element);
```

```
public class Stack<E> implements Collection<E>
    public E peek (); // returns null if stack is empty
    public E pop (); // returns null if stack is empty
    public E push (E element);
```

```
public interface Map<K, V>
    // Implementations: HashMap, TreeMap, LinkedHashMap
    public V get(K key); // returns null if no such key
    public void put(K key, V value);
    public void remove(K key);
    public Set<Map.Entry<K, V>> entrySet();
```