



EXAMINATIONS — 2012
Trimester 1, MID-TERM TEST

COMP103
Introduction to
Data Structures and Algorithms

Time Allowed: 45 minutes

- Instructions:**
1. Attempt **all** of the questions.
 2. *Read each question carefully before attempting it.*
 3. This test will be marked out of **45** marks (i.e. allocate one minute per mark).
 4. Write your answers in the boxes in this test paper and hand in all sheets.
 5. Documentation on some relevant Java classes, interfaces, and exceptions can be found at the end of the paper.

Questions	Marks
1. Collections	[6]
2. Implementing a Stack	[19]
3. Sorting	[10]
4. Recursion	[10]

SPARE PAGE FOR EXTRA ANSWERS

Cross out rough working that you do not want marked.
Specify the question number for work that you do want marked.

Question 1. Collections

[6 marks]

(a) [6 marks] In the boxes below give a short (e.g. one sentence) description for each of the following collections identifying their *key feature(s)*.

Bag

Set

Map

Stack

Queue

List

Question 2. Implementing a Stack

[19 marks]

(a) [8 marks] Complete the following class that implements a Stack using an array. Note that `pop()` should through an `EmptyStackException` if the stack is empty.

```
public class Stack<E> {
    static int INITIAL_CAPACITY = 2;
    E[] data;

    public Stack() {

    }

    public void push(E item) {

    }

    public E pop() {

    }

}
```

(Question 2 continued on next page)

(Question 2 continued)

(b) [6 marks] Write an iterator for your `Stack` class above that is defined as a private inner class and goes through the items in the stack *from the top to the bottom* - in other words, the *first* item should be the one that would have come off *first* if a `pop` method were to be called. For simplicity, assume that you don't need to implement the `remove` method and that you don't need to worry about anyone modifying the `Stack` while you are iterating through it.

```
import java.util . Iterator ;
public class Stack<E> implements Iterable<E> {
    // CODE FROM PREVIOUS SUBQUESTION IMPLEMENTING STACK
    public Iterator <E> iterator() {
        return new StackIterator<E>(this);
    }
    private class StackIterator <E> implements Iterator<E> {
        Stack<E> stack;
        int position;

        public StackIterator (Stack<E> stack) {

        }

        public boolean hasNext() {

        }

        public E next() {

        }

        public void remove() { throw new UnsupportedOperationException(); }
    }
}
```

(Question 2 continued on next page)

(Question 2 continued)

(c) [3 marks] What will the following code print when using the Stack you have just implemented?

```
public static void main(String[] a) {  
    Stack<String> ss = new Stack<String>();  
    ss.push("A"); ss.push("B"); ss.push("C");  
    System.out.println(ss.pop() + ss.pop() + ss.pop());  
    for (String s : ss)  
        System.out.println(s);  
    System.out.println("-----");  
}
```

(d) [2 marks] What is the best order of items when iterating through a Stack? Justify your answer.

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Question 3. Sorting

[10 marks]

(a) [3 marks] Consider the *insertion sort* as discussed in the lectures. Give an example of an array of 10 elements that would produce the *best* cost behaviour for insertion sort and explain briefly why.

(b) [3 marks] Consider the *insertion sort* as discussed in the lectures. Give an example of an array of 10 elements that would produce the *worst* cost behaviour for insertion sort and explain briefly why.

(c) [2 marks] What does it mean for a sorting algorithm to be *stable*?

(d) [2 marks] Imagine you are given two sorting algorithms: one that has worst cost $O(n \log(n))$ and one that has worst cost $O(n^2)$. Which of these two algorithms is going to sort 1 trillion integers faster? Justify your answer.

Question 4. Recursion

[10 marks]

(a) [4 marks] Fix the recursive code below that tries to calculate a factorial. A reminder: $n! = 1 * 2 * \dots * (n - 1) * n$.

```

public int factorial ( int n) {
    if (n > 1) {
        return n * factorial (n);
    } else {
        return 1;
    }
}

```

(b) [4 marks] Write a recursive function that returns the n th Fibonacci number. A reminder that Fibonacci sequence is as follows: $1, 1, 2, 3, 5, 8, \dots, f_{n-2}, f_{n-1}, f_n, \dots$ where $f_n = f_{n-1} + f_{n-2}$.

```

public int fib ( int n) {

}

```

(c) [2 marks] Explain why your recursive version of fib is particularly inefficient. Justify your answer.

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Appendix (may be removed)

Brief (and simplified) specifications of some relevant interfaces and classes.

public class *Scanner*

```
public boolean hasNext(); // there is more to read
public String next(); // return the next token (word)
public String nextLine(); // return the next line
public int nextInt (); // return the next integer
```

public class *Random*

```
public int nextInt(int n); // return a random integer between 0 and n-1
public double nextDouble(); // return a random double between 0.0 and 1.0
```

public interface *Iterator* <*E*>

```
public boolean hasNext();
public E next();
public void remove();
```

public interface *Iterable* <*E*>

```
public Iterator <E> iterator();
```

// Can use in the "for each" loop

public interface *Comparable* <*E*>

```
public int compareTo(E o);
```

// Can compare this to another *E*

public interface *Comparator* <*E*>

```
public int compare(E o1, E o2);
```

// Can use this to compare two *E*'s

```
public class Collections
    public void sort(List<E>, Comparator<E>)
```

```
public interface Collection<E>
    public boolean isEmpty();
    public int size ();
    public boolean add();
    public Iterator <E> iterator();
```

```
public interface List<E> extends Collection<E>
    // Implementations: ArrayList
    public E get(int index);
    public void set(int index, E element);
    public void add(E element);
    public void add(int index, E element);
    public void remove(int index);
    public void remove(Object element);
```

```
public interface Set extends Collection<E>
    // Implementations: HashSet, SortedSet, TreeSet
    public boolean contains(Object element);
    public boolean add(E element);
    public boolean remove(Object element);
```

```
public interface Queue<E> extends Collection<E>
    // Implementations: LinkedList, PriorityQueue
    public E peek (); // returns null if queue is empty
    public E poll (); // returns null if queue is empty
    public boolean offer (E element);
```

```
public class Stack<E> implements Collection<E>
    public E peek (); // returns null if stack is empty
    public E pop (); // returns null if stack is empty
    public E push (E element);
```

```
public interface Map<K, V>
    // Implementations: HashMap, TreeMap, LinkedHashMap
    public V get(K key); // returns null if no such key
    public void put(K key, V value);
    public void remove(K key);
    public Set<Map.Entry<K, V>> entrySet();
```